

Complex Logarithm QUESTION 9/2/23

$$\log_{10} (x-1) + 2 = \log_{10} (3x+2) + \log_{10} 25$$

Rearrange the equation to equal to 2

$$= \log_{10} (3x+2) + \log_{10} 25 - \log_{10} (x-1) = 2$$

$$= \log_{10} (3x+2) + \log_{10} 25 - \log_{10} (x-1) = 2 \cdot \log_{10} 10$$

$$= \log_{10} (3x+2) + \log_{10} 25 - \log_{10} (x-1) = \log_{10} 10^2$$

$$= \log_{10} (3x+2) + \log_{10} 25 - \log_{10} (x-1) = \log_{10} 100$$

$$= \log_{10} (3x+2)(25) - \log_{10} (x-1) = \log_{10} 100$$

Now divide the two since we have the same base

$$= \frac{\log_{10} (75x+50)}{x-1} = \log_{10} 100$$

Now simplify since the bases are the same

$$= \frac{75x+50}{x-1} = 100$$

$$= 100x - 100 = 75x + 50$$

$$= 100x - 75x = 50 + 100$$

$$= 25x = 150$$

Since when you multiply 25 by a number you get 150 then $x = \frac{150}{25} = 6$